# CS 428: Fall 2009 Introduction to Computer Graphics 

## Visibility

## Visibility

- Also known as hidden surface removal
- Respect the nature of occlusion in visual scenes

yes

- Algorithms for determining which parts of the object/surfaces are visible
- For now only opaque objects


## Visibility algorithms

- Occlusion
- More than one point projects to the same point in the image
- Obviously, the point closest to the observer is visible
- Unless the closest point is (semi)transparent, in which case objects behind become visible



## Visibility algorithms

- Complexity
- Visibility computation is comparable to sorting
- Worst case complexity is worse
- Given a scene with $\mathbf{n}$ polygons, there might exist $\sim \mathbf{n}^{2}$ visible parts
- Worst case complexity is
 O( $\mathbf{n}^{2}$ )


## Visibility

- A variety of algorithms
- Each work better (more efficiently) in different situations
- Two main categories
- Object precision algorithms
- Image precision algorithms


## Object precision

- Operate on geometric primitives
- For every object in the scene
- Compute visible part (not occluded by any other object in the scene) $\rightarrow$ needs high precision
- Draw visible part
- Results are independent of display resolution
- Brute force algorithm is $\mathbf{O}\left(\mathbf{n}^{2}\right)$
- $\mathrm{n}=$ number of objects on screen
- Can be improved (pre-computation) to O(n log n)


## Object precision

- Hard(er) to implement
- Due to numerical error
- Due to tricky geometric computations (intersections, Boolean operations, etc.)



## List priority methods

- Draw surfaces in back-to-front order

- Painters algorithm



## List priority methods

- Problem:
such an ordering does not always exist



- In such cases, polygons must be split
- This can result in many split polygons (see worst case complexity)


## List priority methods

- Observation: polygons are drawn in the correct order if



- For every polygon part P
- Draw everything behind $\mathbf{P}$
- Draw $\mathbf{P}$
- Draw everything in front of $\mathbf{P}$

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## Binary space partion (BSP)

- BSP tree: binary spatial subdivision
- A tree that encodes viewpoint-independent and relative position/depth information
- Every node is a splitting plane, which cuts space into two parts (two half-spaces)
- Leads to an ordering with respect to every line in 2D (plane in 3D, etc.)
- For visibility, the splitting (hyper)planes are defined by the scene geometry


## Binary space partion (BSP)



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## Binary space partion (BSP)

- Ordered list of polygons by traversal
- Identify half-space $\mathbf{H}$ of eye position
- Traversal ordering
- Other half-space
- Polygon (node)
- Containing half-space H


## Binary space partion (BSP)



## Binary space partion (BSP)

- Some issues
- Which plane to chose as the splitting plane in each step?
- How to balance the tree?
- How to avoid excessive polygon splitting?
- Solution
- Re-run the algorithm!
- "Perfect" BSP is in NP (exponential complexity)
- Randomized version works well, has good expected performance


## Image precision

- You already know one: z-buffer
- Z-buffer algorithm is an output sensitive algorithm (only looks at rendered pixels)
- Brute force
- For each pixel
- Find object closest to camera which projects to here
- Draw that object
- Complexity is $\mathbf{O}(\mathrm{nP})$, while z-buffer is $\mathbf{O}\left(\mathrm{nP}_{\mathrm{R}}\right)$


## Image precision

- You already know one: z-buffer
- Z-buffer algorithm is an output sensitive algorithm (only looks at rendered pixels)
- Z-Buffer
- Initialize depth image D to farthest distance
- For each pixel $\mathbf{p}$ of each polygon with depth $\mathbf{d}$
- If $d(x, y)<D(x, y)$
- Replace $D(x, y)$ with $d(x, y)$ and write color of $p$ into image


## Ray casting

- Preview for next lecture
- Associate a ray with each pixel

- Find object-ray intersection points
- Choose closest point to the camera

