

CS 428: Fall 2010

Introduction to Computer Graphics

Polygonal rendering: illumination

Polygon shading

- Non-global illumination
 - No shadows, refraction, inter-object reflection...
- Describing light
 - Units – don't worry for now, just use ratio

light exiting surface towards viewer
light incident on surface from lights

Polygon shading

- Describing light

- Units – don't worry for now, just use ratio

light exiting surface towards viewer
light incident on surface from lights

- Depends on

- Physical material/surface properties
- Geometric relation between lights, surface and viewer
- Color and intensity of lights in the scene
- Hard to define these properties precisely



Bidirectional reflection distribution function (**BRDF**)

- Describes reflection of light
- Spectral reflection factor
- Ratio of reflected radiance L to incident irradiance E

$$\rho(\lambda, \phi_r, \theta_r, \phi_i, \theta_i) = \frac{L_{\lambda,r}(\lambda, \phi_r, \theta_r)}{E_{\lambda,i}(\lambda, \phi_i, \theta_i)} = \frac{L_{\lambda,r}(\lambda, \phi_r, \theta_r)}{\int L_{\lambda,i}(\lambda, \phi_i, \theta_i) \cos(\theta_i) d\Omega_i}$$

- Incident irradiance: Index i
- Reflected radiance: Index r

Bidirectional reflection distribution function (BRDF)

1. Reciprocity

- ρ_λ does not change, when switching incident and reflected direction

2. ρ_λ is generally anisotropic

- Rotation about the surface normal changes ρ_λ
- Typical examples are cloth or brushed metal

3. Superposition

- Light from various directions can be linearly added
- Integrating over all incident directions leads to

$$L_{\lambda,r} = \int_{\Omega_i} \rho L_{\lambda,i} \cos(\theta_i) d\Omega_i$$

Bidirectional reflection distribution function (**BRDF**)

- Reflection factor is always positive
- In CG we use the reflection ratio r
 - Applied to luminance/brightness
 - Dimensionless

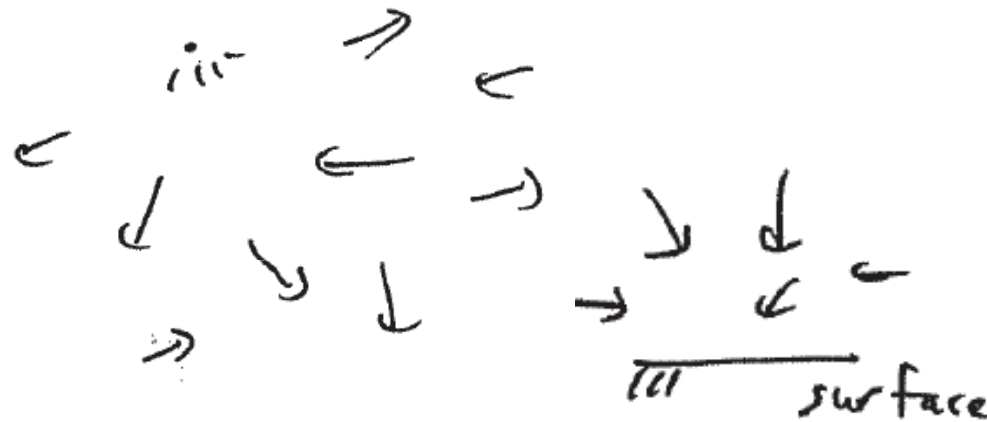
light exiting surface towards viewer
light incident on surface from lights

Illumination models

- Not physics-based
 - rather an approximation which is more computationally tractable
- **Ambient** reflection
- **Diffuse** reflection
- **Specular** reflection
- All use a **point** light source
 - $(x, y, z) + \text{Intensity } (I_r, I_g, I_b)$

Ambient reflection

- Light scattered in scene – uniformly



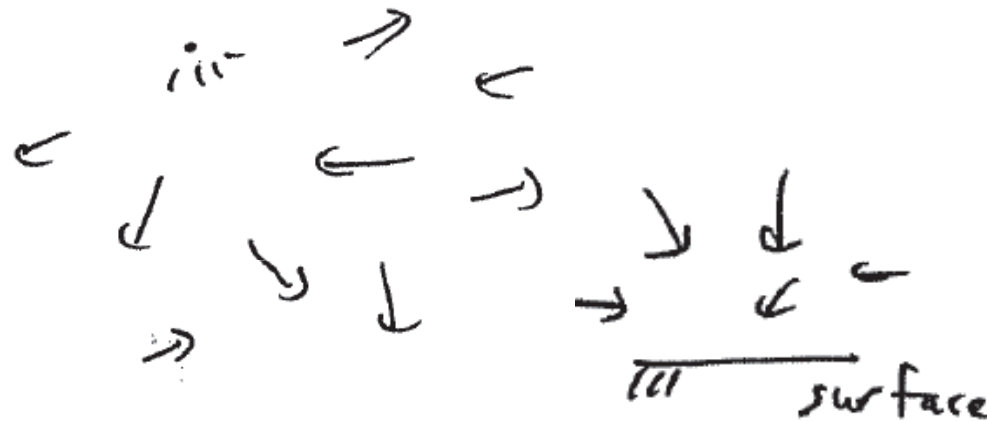
$$I_{\text{ambient}} = L_a k_a$$

Intensity of ambient light

fraction of ambient light reflected $\in [0, 1]$

Ambient reflection

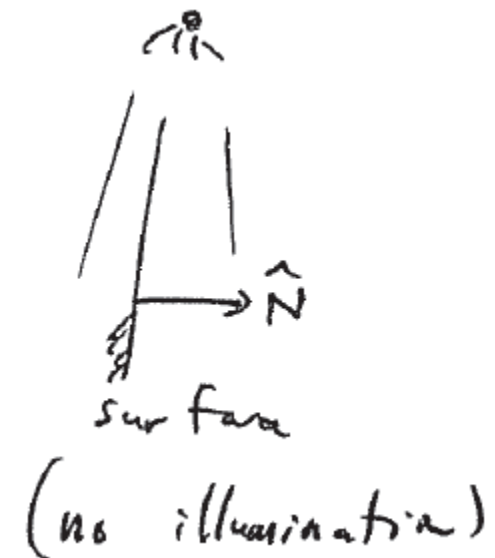
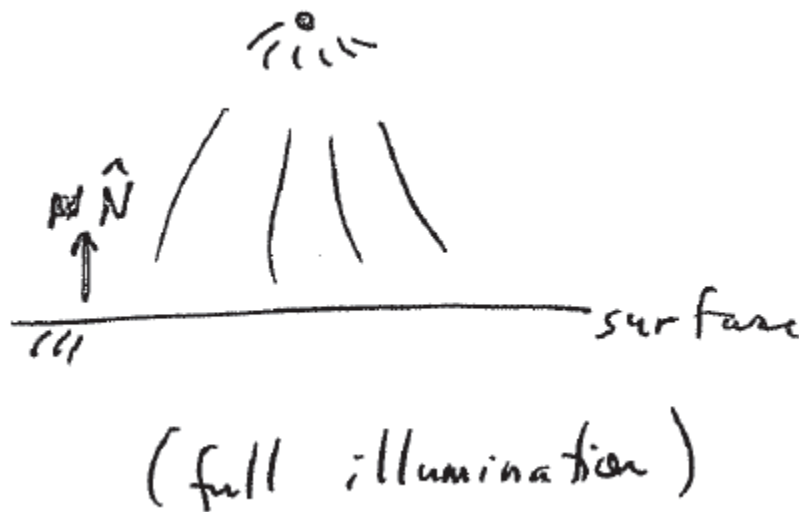
- Light scattered in scene – uniformly



- Independent of light, viewer + surface position
- *Hack* to get some global illumination effects
- Without this term, images have too much contrast

Diffuse (Lambertian) reflection

- Typical of dull, matte surfaces → rough
- Independent of viewer position
- Dependent on light position



Diffuse (Lambertian) reflection

- Lamberts cosine law



$$I_{\text{diffuse}} = L_d k_d \cos \theta = L_d k_d (\hat{n} \cdot \hat{l})$$

intensity of point light source

diffuse reflection coeff of surface $\in [0, 1]$

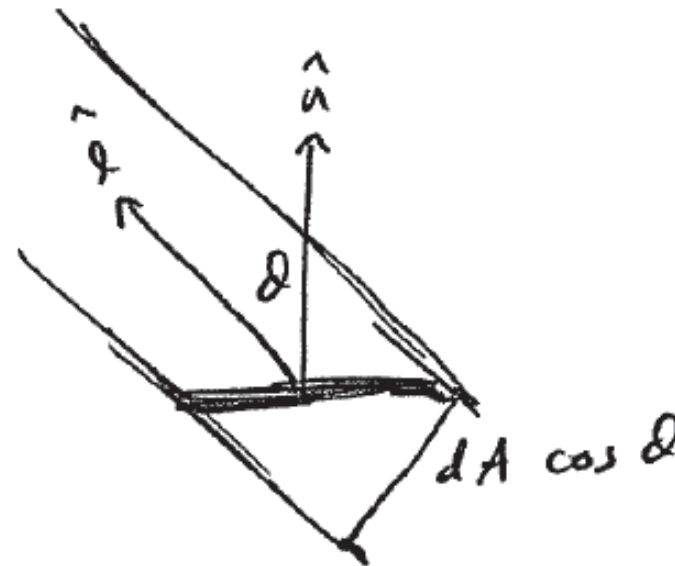
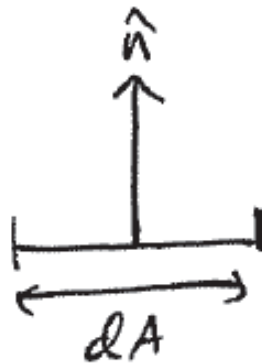
Diffuse (Lambertian) reflection

- Lamberts cosine law

$$L_d = k_d \cdot \max(0, \cos \theta)$$

for when surface
faces the other way

- Geometric intuition



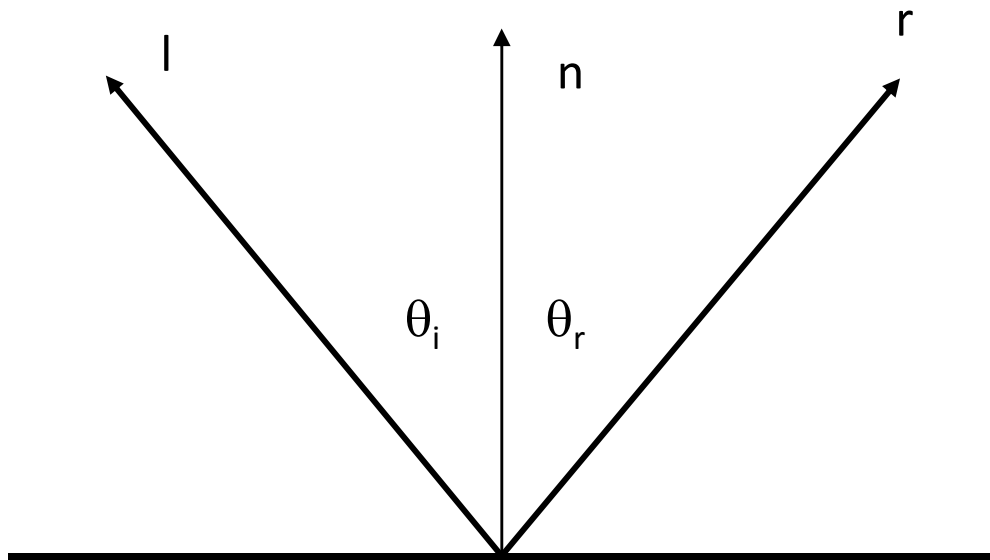
Ideal reflection

- Mirror reflection by law of reflection
 - The incident and reflected ray form the same angle with the surface normal
 - The incident and reflected ray and surface normal all lie in the same plane
 - In polar coordinates: $\theta_r = \theta_i$ and $\phi_r = \phi_i + \pi$
 - For view ray \mathbf{l} and (normalized) normal \mathbf{n}

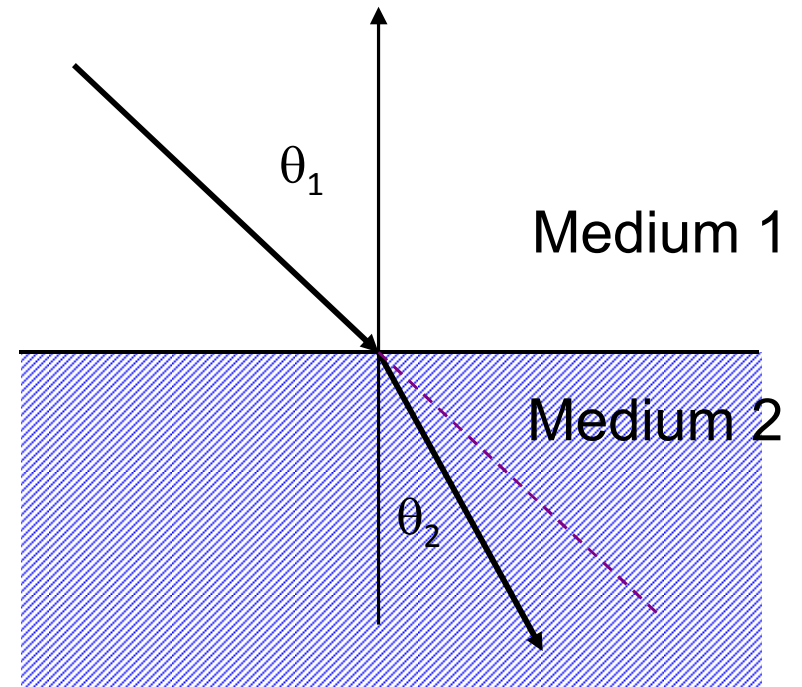
$$\mathbf{r} = -\mathbf{s} + 2 (\mathbf{s} \cdot \mathbf{n}) \mathbf{n}$$

Ideal reflection

Geometry of Reflection law



Geometry of refraction law



Ideal reflection

Law of refraction

- The incident and refracted ray and surface normal all lie in the same plane
- Sine of the incident angle has a constant ratio to the sine of the refraction angle
 - This ratio is dependent on the nature of the participating media

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \Leftrightarrow \frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1} = \text{const.}$$

- n_1 and n_2 are the indices of refraction
 - Defined as the ratio of light speed in vacuum to light speed in the participating media

Ideal reflection

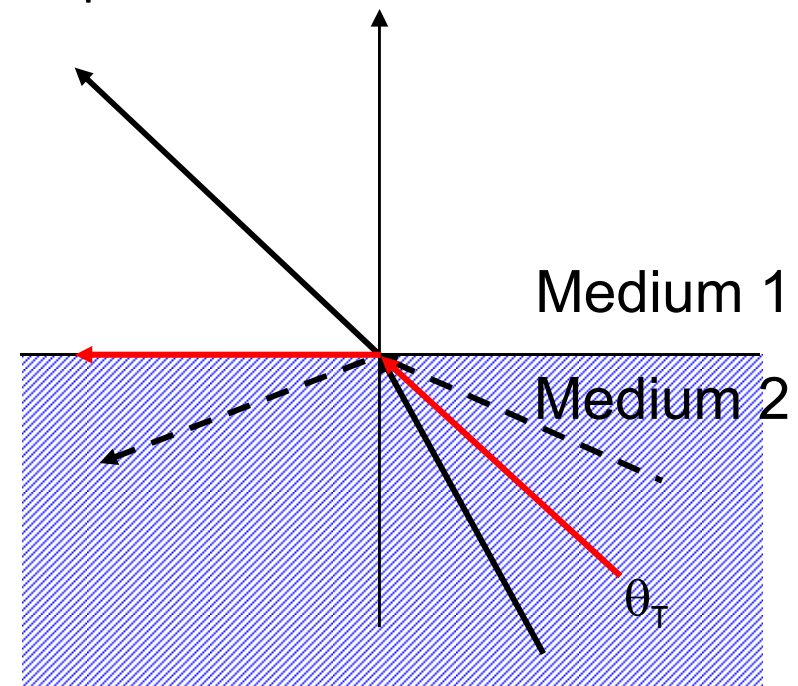
Total reflection

- Transition from optically dense to less dense material $n_2 < n_1$

- Rays refracted away from the surface normal
- There exists an incident angle θ_T with refraction angle of 90°

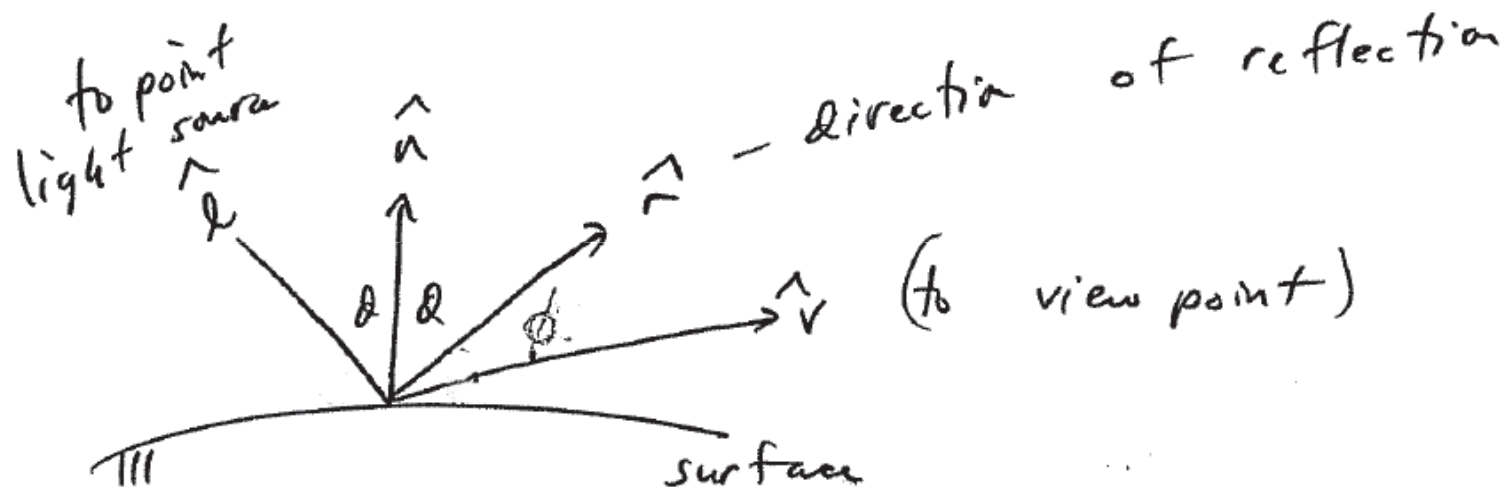
$$\sin \theta_T = \frac{n_2}{n_1}.$$

- Once θ_T is exceeded
- All light reflected on the boundary between media
- Total reflection



Specular reflection

- Directed reflection from shiny surfaces

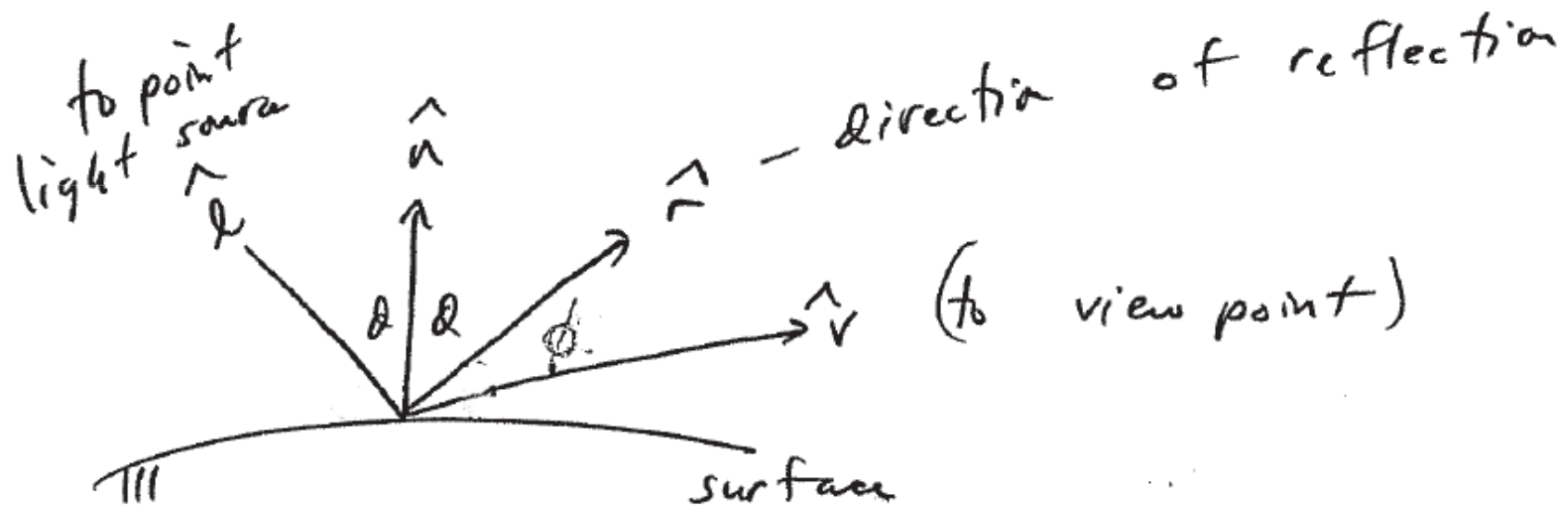


- Resulting color is a combination of surface color + light color



Specular reflection

- Directed reflection from shiny surfaces

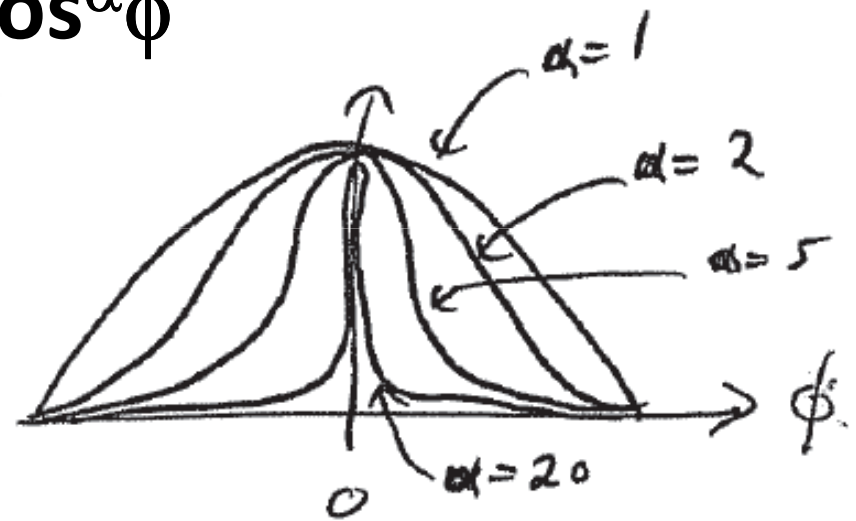


- More reflection as ϕ goes to 0

Specular reflection

Phong reflection

- More reflection as ϕ goes to 0
 - Not just $\cos \phi \rightarrow$ use $\mathbf{cos}^\alpha \phi$
 - As α increases surface looks shinier
 - α is surface property



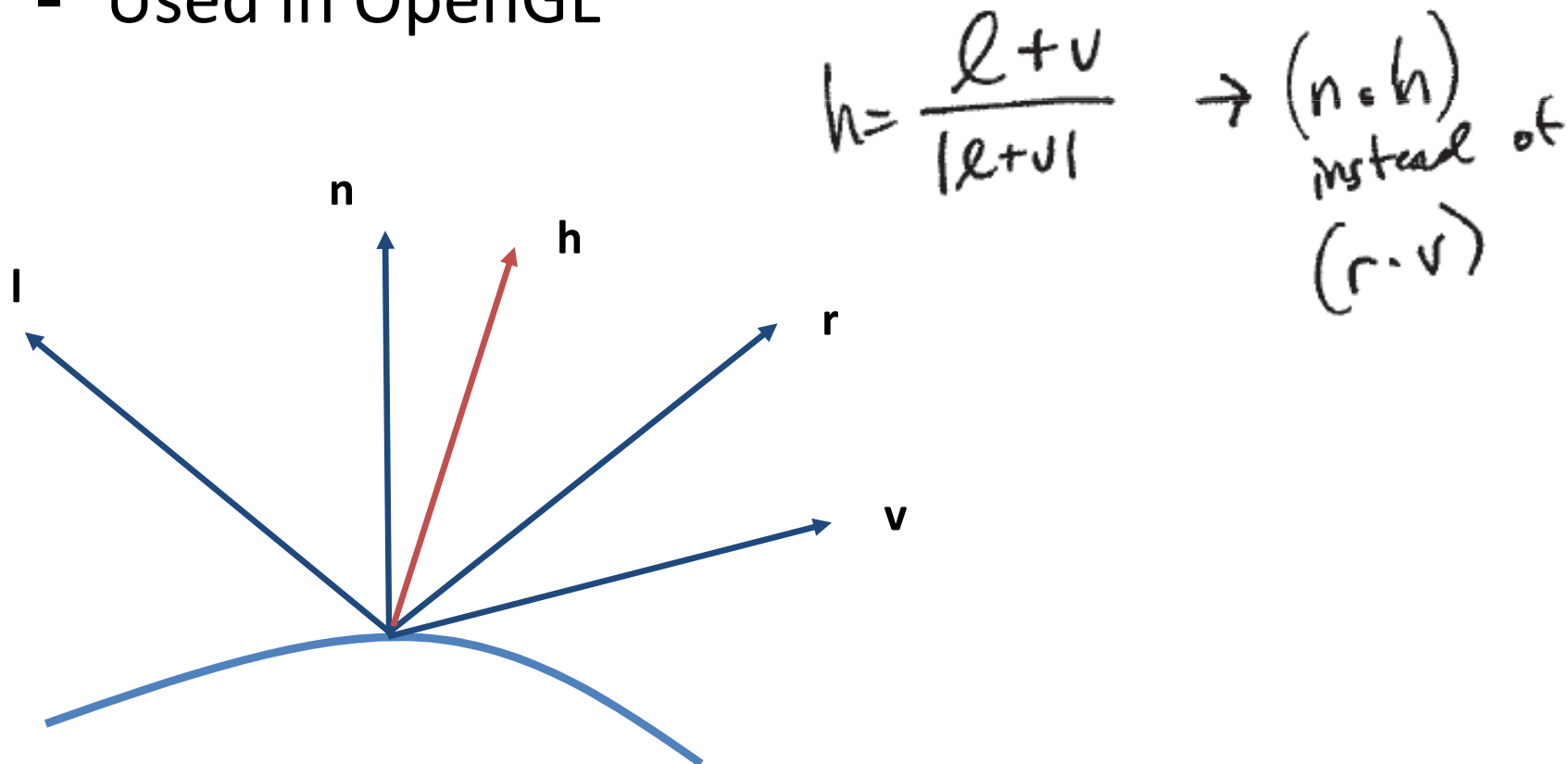
$$I_{\text{specular}} = L_s k_s (\hat{r} \cdot \hat{v})^\alpha$$

spec reflc coeff $\in [0, 1]$

Specular reflection

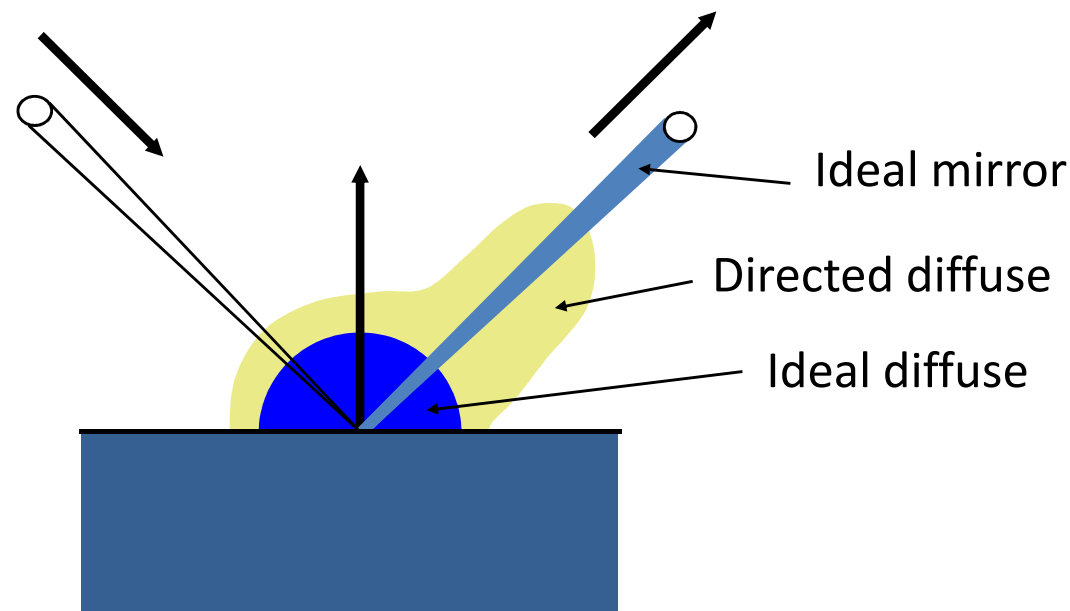
Blinn-Phong reflection

- Use halfway vector instead
 - Somewhat more efficient (less operations)
 - Used in OpenGL



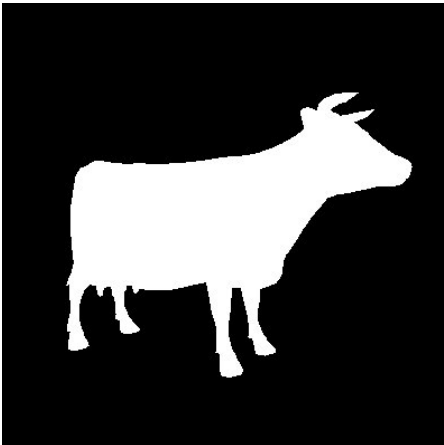
Directed diffuse reflection

- Ideal reflectors (Lambert or mirror) seldom
- Heuristic to model the real BRDF
- Combination of ambient, diffuse and specular
 - Should add to 1 (careful when selecting coeffs!)

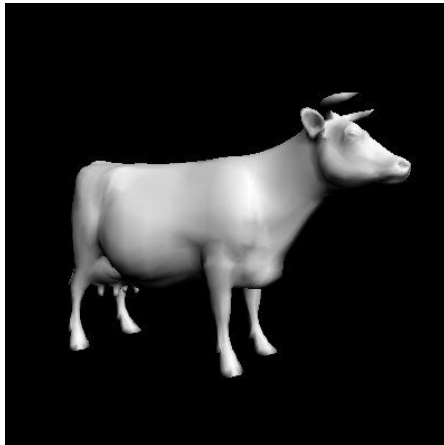


Combination

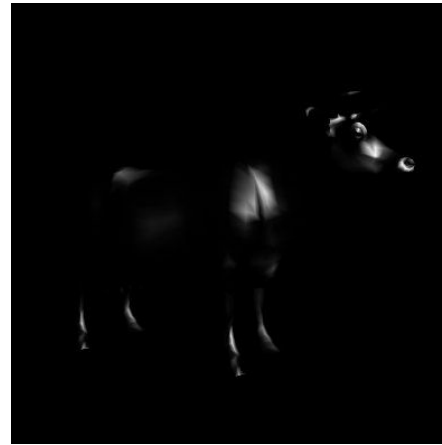
ambient



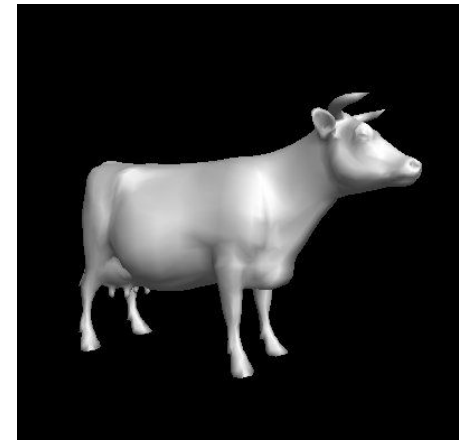
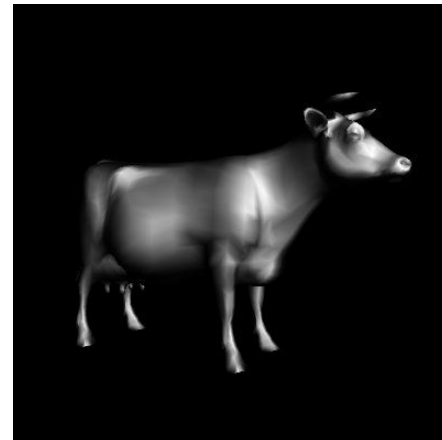
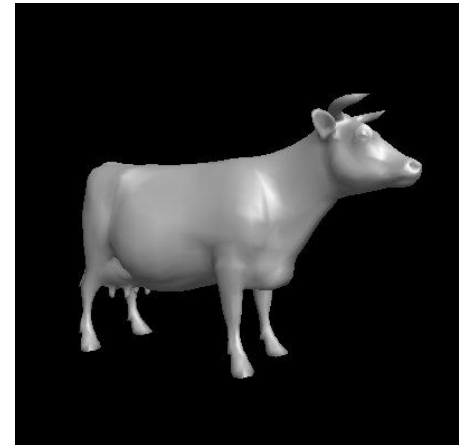
diffuse



specular



all



OpenGL details

- Colored lights and surfaces
- Also, light colors for each of the types of lighting, and each light source

OpenGL details

```
// light and material
float mat_ambient[] = { 0.5f, 0.5f, 0.5f, 1.0f };
float mat_specular[] = { 0.6f, 0.6f, 0.6f, 1.0f };
float mat_shininess[] = { 3.0f };
float model_ambient[] = { 0.3f, 0.3f, 0.3f };
float light_position[] = { 5.0f, 5.0f, 5.0f, 0.0f };
glMaterialfv(GL_FRONT, GL_AMBIENT, mat_ambient);
glMaterialfv(GL_FRONT, GL_SPECULAR, mat_specular);
glMaterialfv(GL_FRONT, GL_SHININESS, mat_shininess);
glLightfv(GL_LIGHT0, GL_POSITION, light_position);
glLightModelfv(GL_LIGHT_MODEL_AMBIENT, model_ambient);
glEnable(GL_LIGHTING);
glEnable(GL_LIGHT0);
```


Polygon mesh shading

- Each polygon independent, shaded separately

- Three ways to do this



- **Constant** – faceted. Single color per polygon
- **Gouraud** – intensity interpolation
- **Phong** – surface normal interpolation

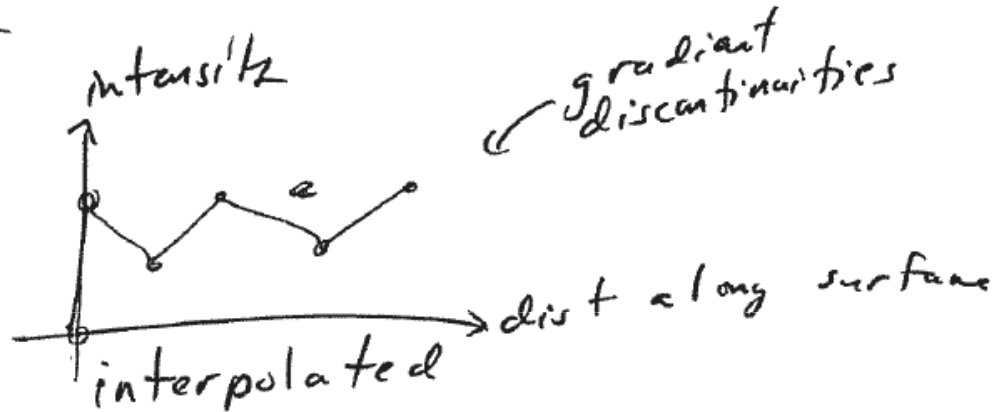


Polygon mesh shading

Mach banding effects



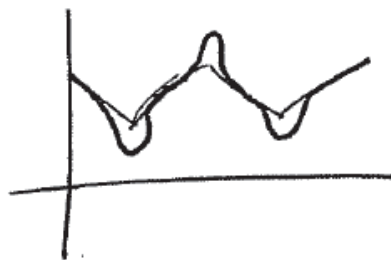
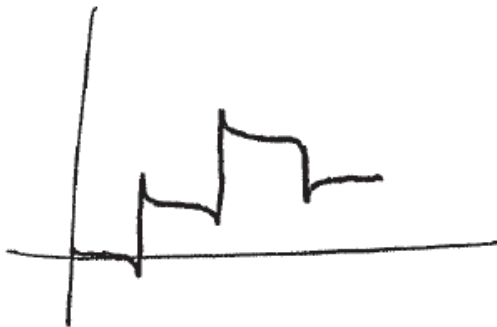
faceted



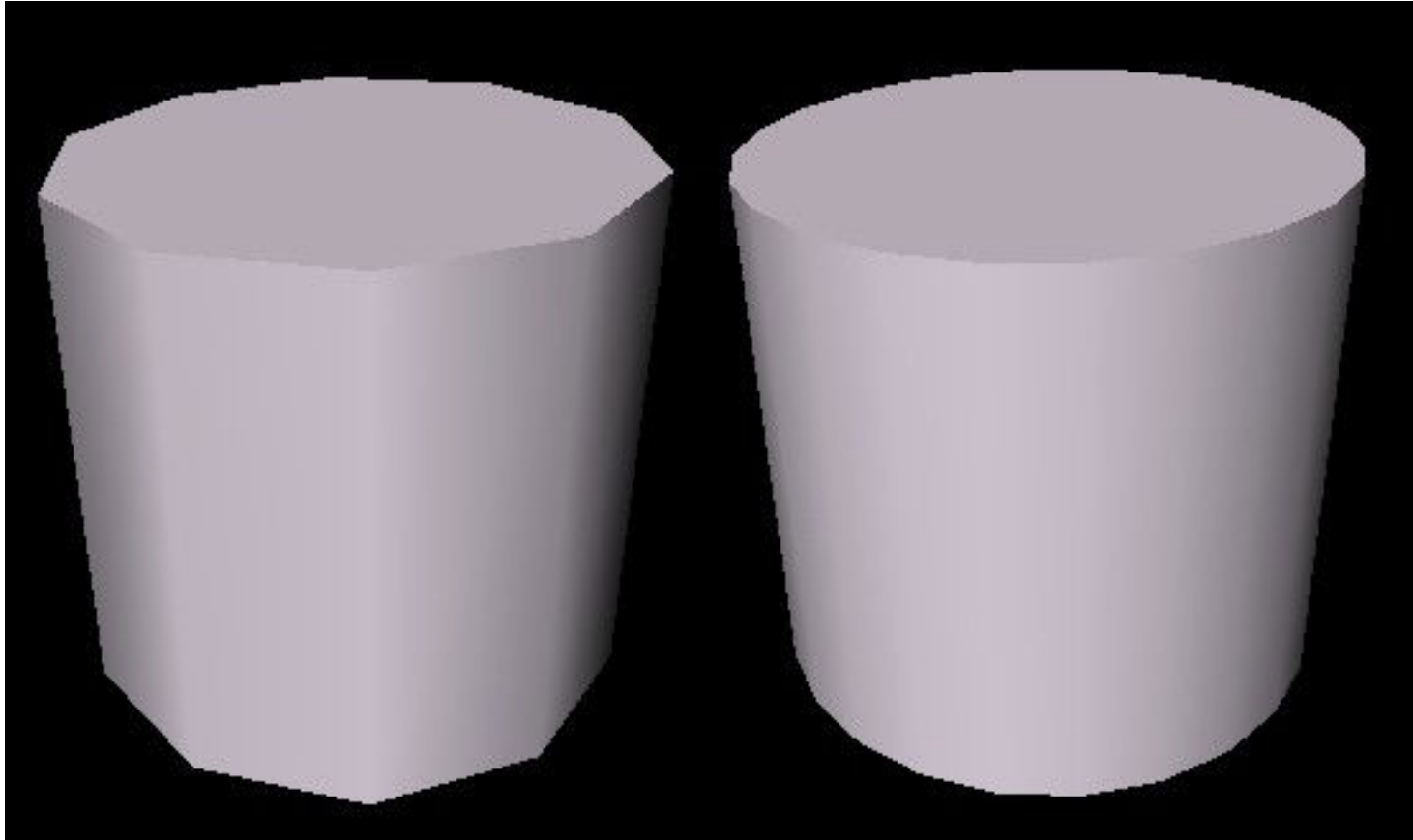
interpolated



perceived



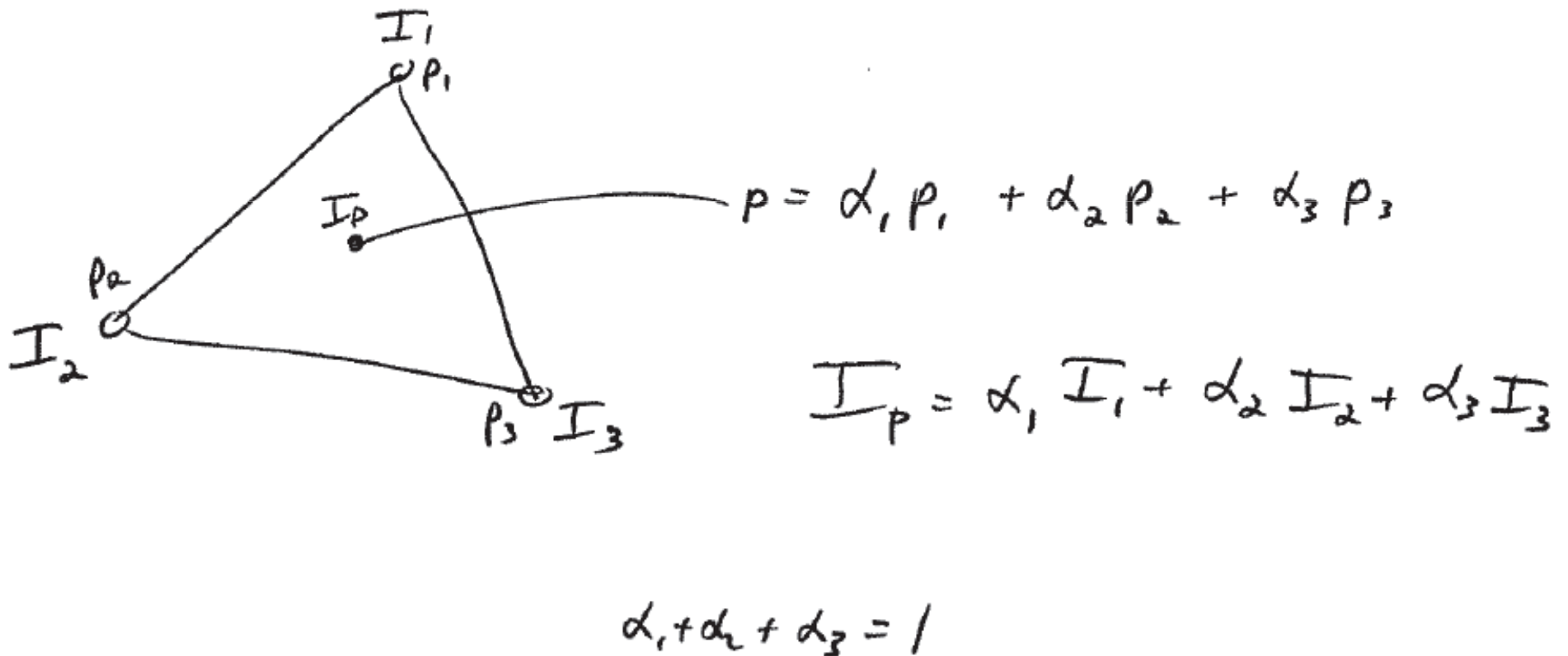
Gouraud Shading Mach bands



Gets better with more polygons →

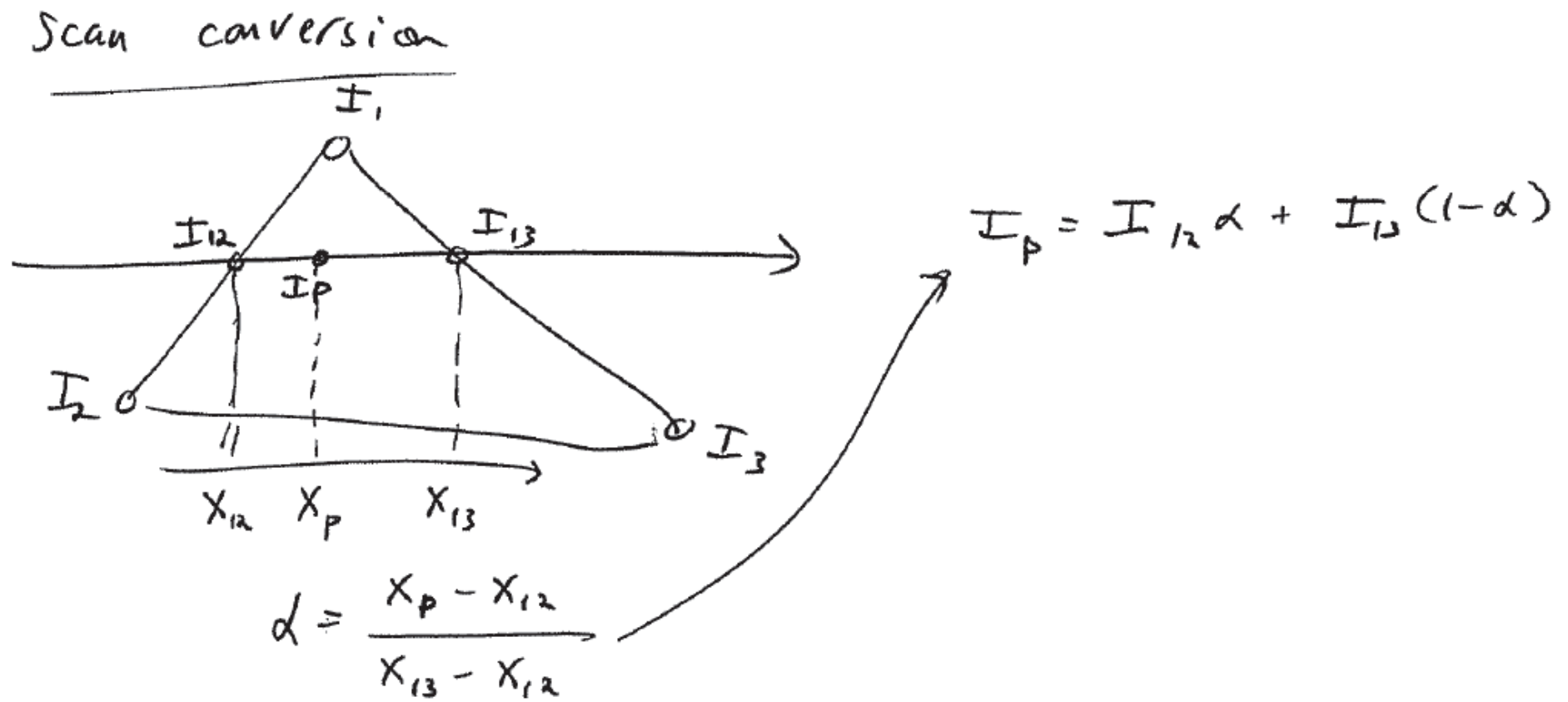
Gouraud shading

- Barycentric interpolation of illumination

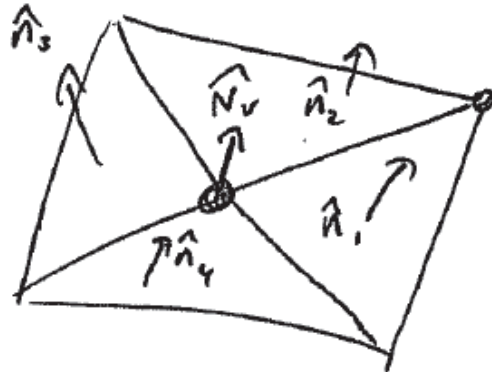


Gouraud shading


- Barycentric interpolation of illumination

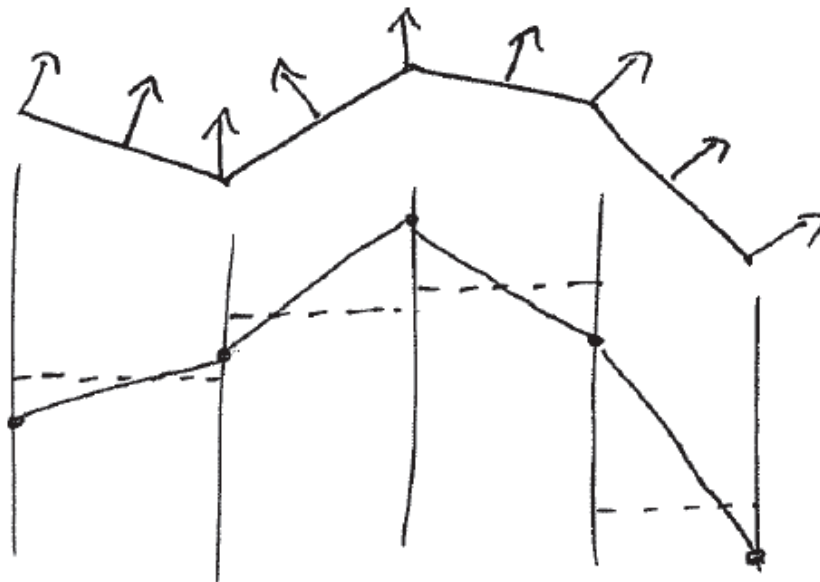


Gouraud shading



$$\hat{n}_v = \frac{\hat{n}_1 + \hat{n}_2 + \hat{n}_3 + \hat{n}_4}{\| \quad \quad \|}$$

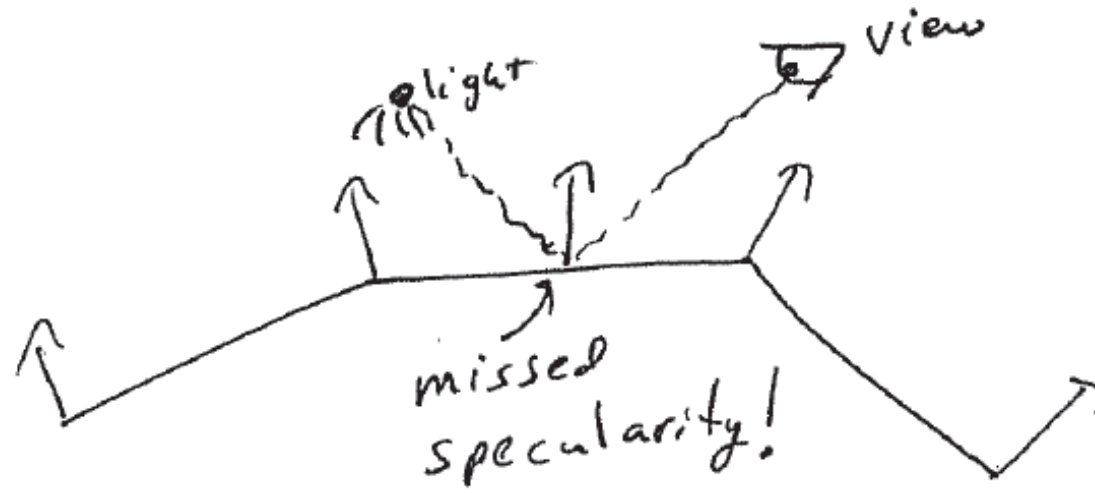
side view 



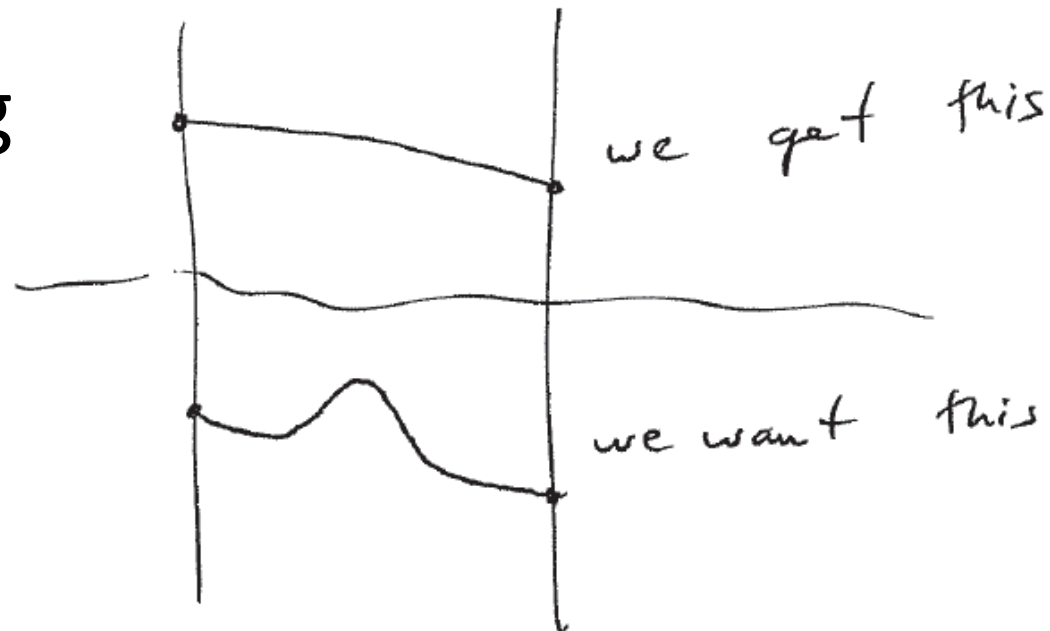
----- constant
————— Gouraud

Gouraud shading

- Problems



- Motion aliasing makes this worse!



Phong shading

- Interpolate normals linearly at each pixel
 - Lighting computation at each pixel
- Looks much better
- More expensive
- Only works in graphics hardware (GLSL etc.)

