CS 428: Fall 2010

Introduction to Computer Graphics

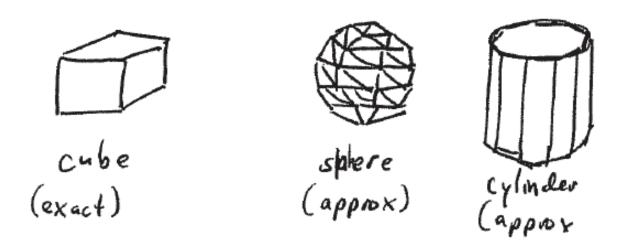
Polygonal meshes

Topic overview

- Image formation and OpenGL
- Transformations and viewing
- Polygons and polygon meshes
 - 3D model/mesh representations
 - Piecewise linear shape approximations
 - Illumination and polygon shading
- Modeling and animation
- Rendering

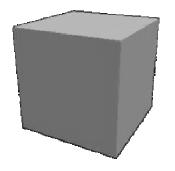
Polygon meshes

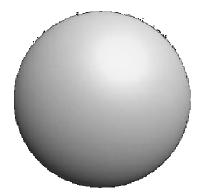
- Some objects are flat
- Some objects are smooth ← approximate!
 - Use many planar triangles/quadrilaterals to approximate the underlying smooth surface



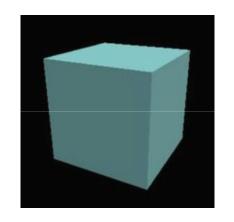
Approximating shapes with polygons

shape

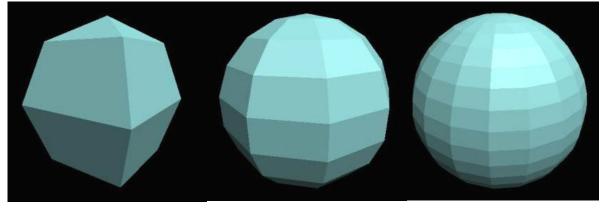




polygon mesh



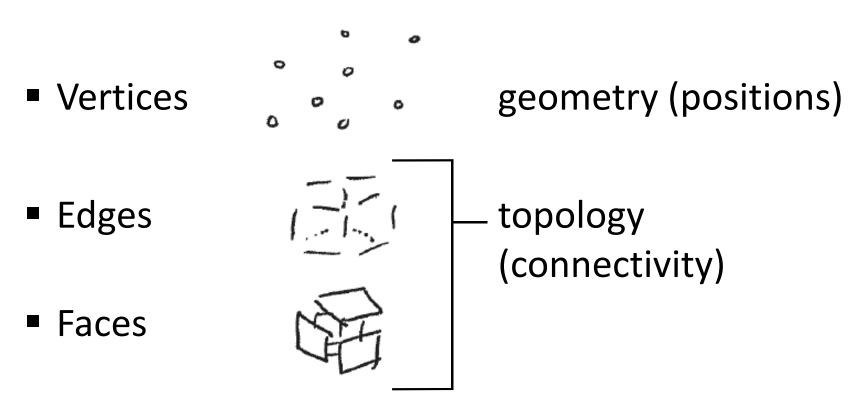
(exact)



(approximated)

Polygon meshes

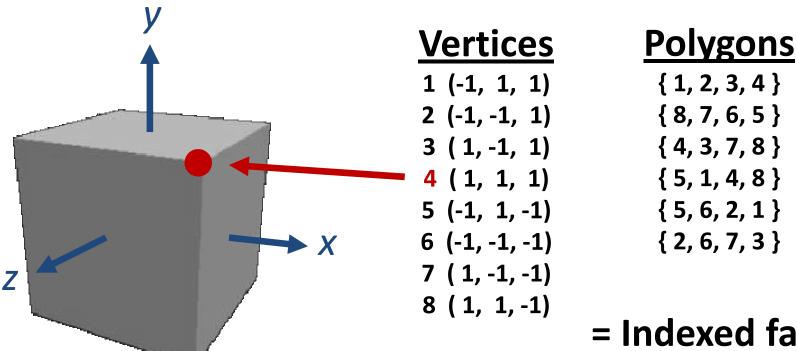
Polygon mesh



 All three are redundant, but can lead to more efficient (neighborhood) computation

Representation

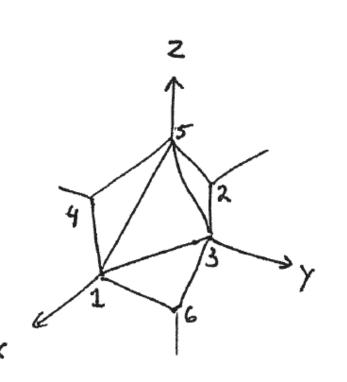
- Often just stored in a file
 - List of vertices (x_1, y_1, z_1) ... (x_n, y_n, z_n) followed by
 - List of polygons = ordered list of indices (1,2,3) ...

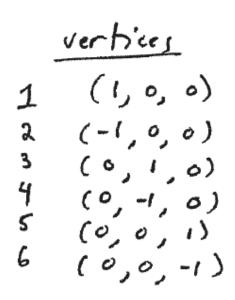


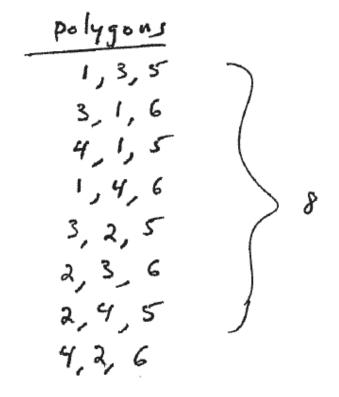
= Indexed face set

Representation

Example: octahedron







Connectivity

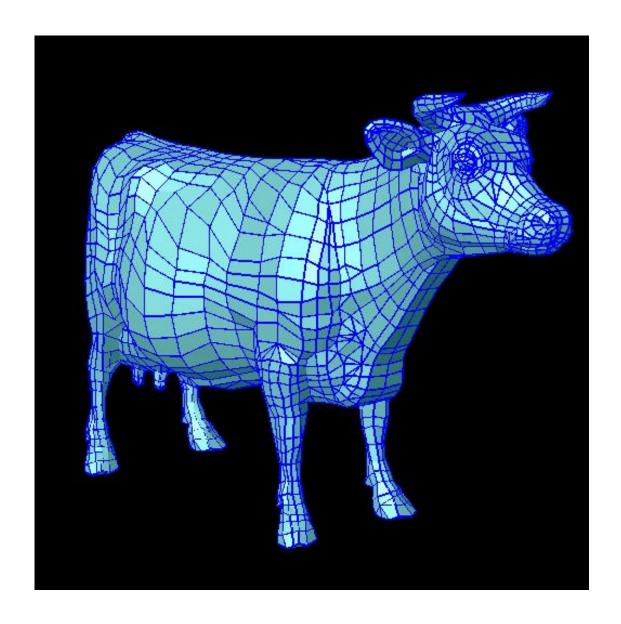
- Vertices and polygons are sufficient for rendering
- When adjacency information is needed
 - Edges: 2 vertices
 - 1 or 2 polygons, assuming no T-joins



- Vertices store list of adjacent vertices, edges or polygons
- Polygons store list of edges
- Sophisticated data structures exist (CS 523)

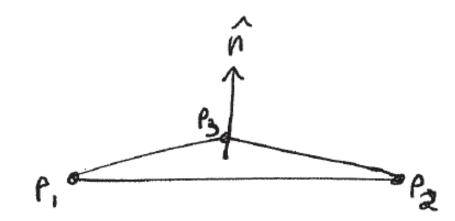
Polygon mesh example

2903 vertices3263 polygons

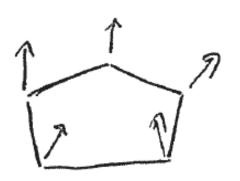


Polygon normals

Triangles have a single normal vector

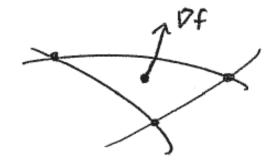


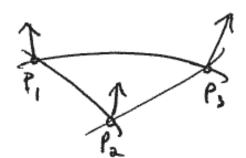
- More than 3 points produces a normal at each vertex
 - If all points in a plane all normals are equal



Polygon normals

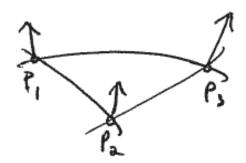
- If the polygon is sampled from a surface, we can compute normals analytically
 - Disance field f(x,y,z) = 0 ... a map from R³ → R
 - The gradient ∇f is the (un-normalized) normal at (x,y,z)
 - But we can find the normals at the vertices here
 - How?





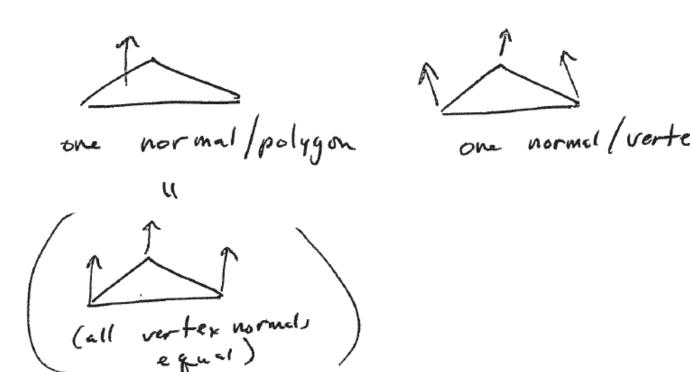
Vertex normals

- Average the normals of adjacent polygons
- For an arbitrary vertex
 - Compute the cross product between each two adjacent outgoing edges (= each adj. polygon)
 - Sum the resulting vectors into a single vector
 - Normalize this vector
- More sophisticated methods exist (CS 523)



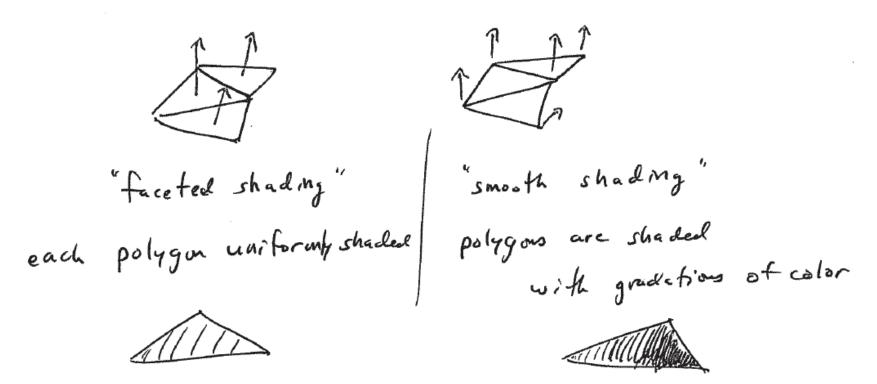
Polygon shading

- For now (more details later): normals are used for shading (= computing brightness values)
- One polygon



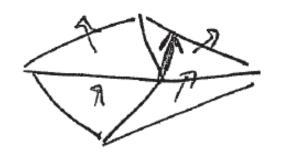
Polygon shading

- For now (more details later): normals are used for shading (= computing brightness values)
- Multiple polygons



Smooth shading

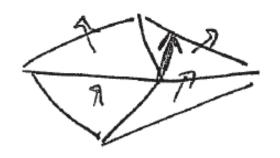
 Find average normal of adjacent polygons

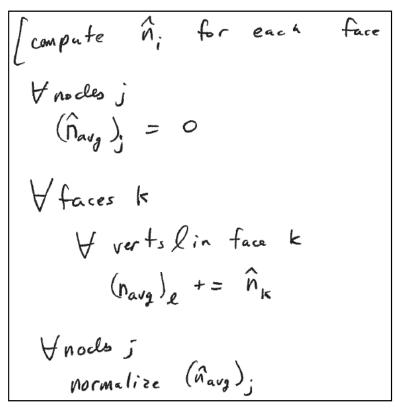


How to compute?

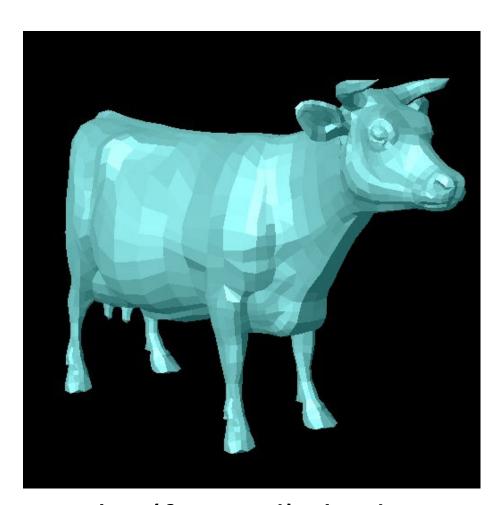
Smooth shading

- Find average normal of adjacent polygons
- Do we need a list of adjacent polygons?
 - Not if we want to compute all avg. normals
- This can be performed from an indexed face set on reading the file

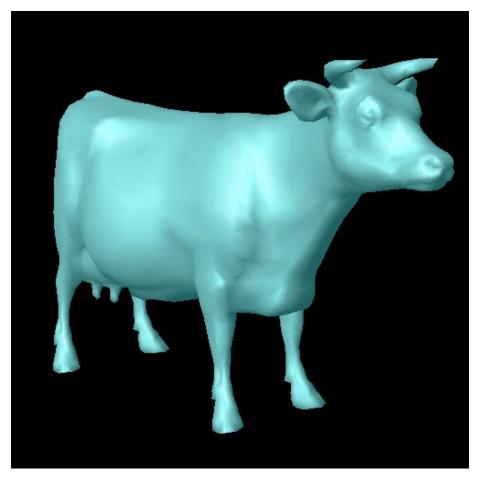




Mesh rendering styles

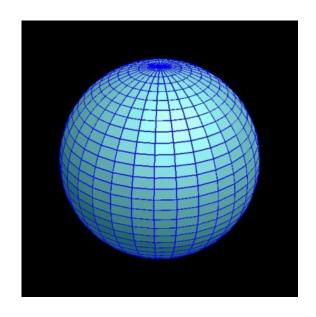


Flat (faceted) shading

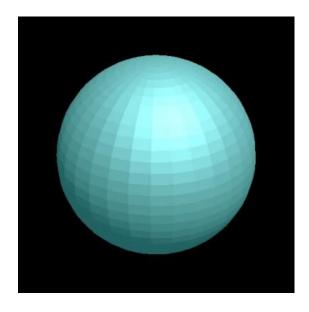


Smooth (Gouraud) shading

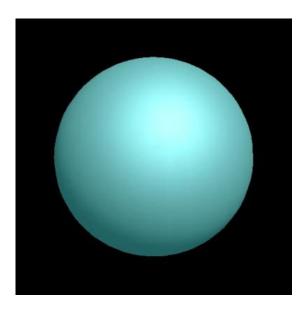
Sphere



Polygons and wireframe



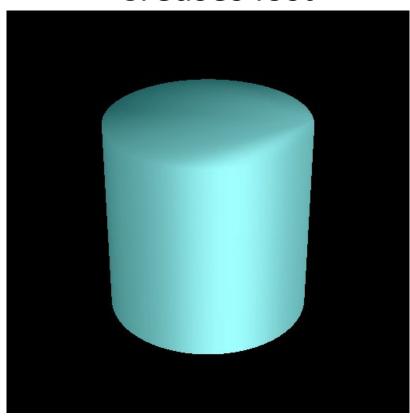
Flat



Smooth

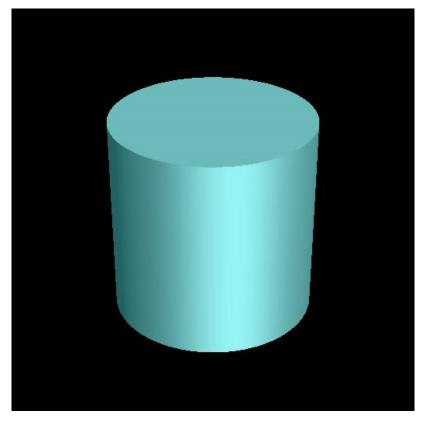
Vertex normals and smooth shading

Creases lost



Normal stored in vertex

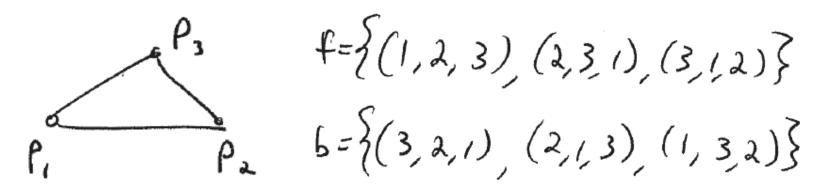
Creases retained



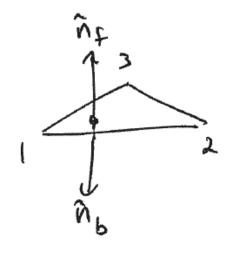
Normals stored in polygon (per vertex)

Polygon/surface orientation

- Order of vertices specifies a polygon
- Backwards and forwards = same polygon



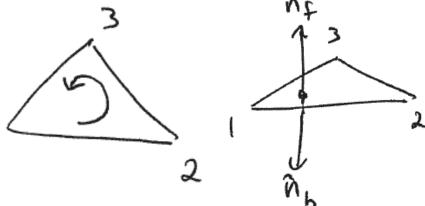
But the normal direction flips



Polygon/surface orientation

Use right-hand rule to determine normal direction

 Counter clockwise: normal comes out of "slide"



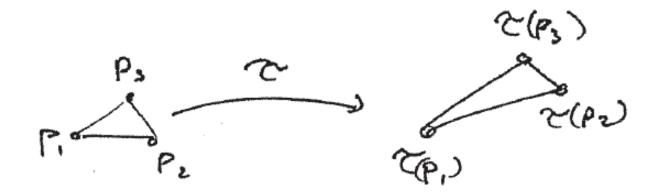
- Convention: list vertices in CCW order
- Mesh should be consistently oriented
 - All point out!





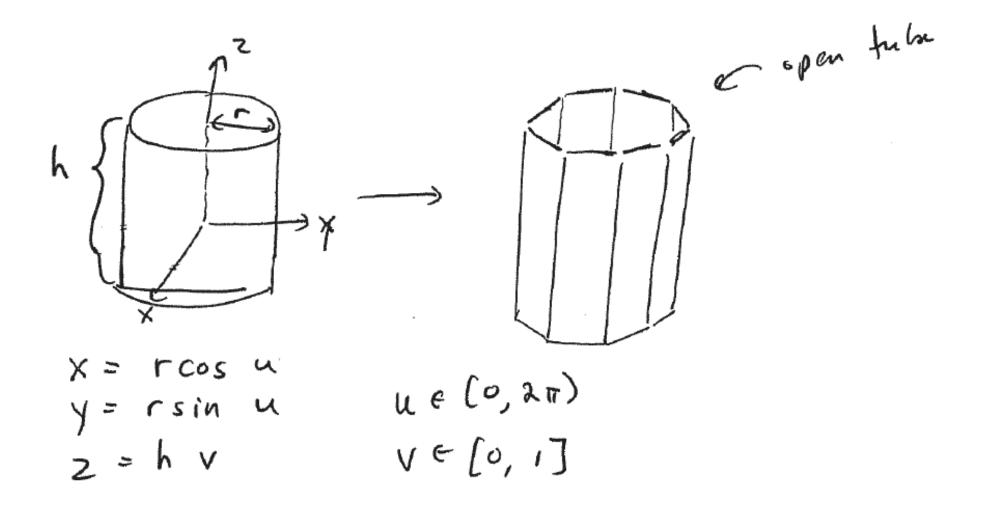
Polygon transformation

Transform points

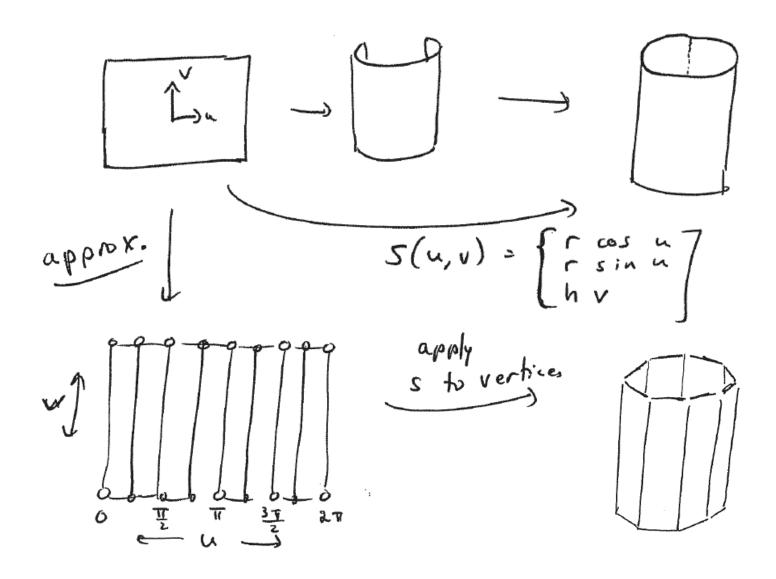


- Draw polygon using these
 - Affine transformations map lines to lines (planes to planes, etc.)

Tessellation

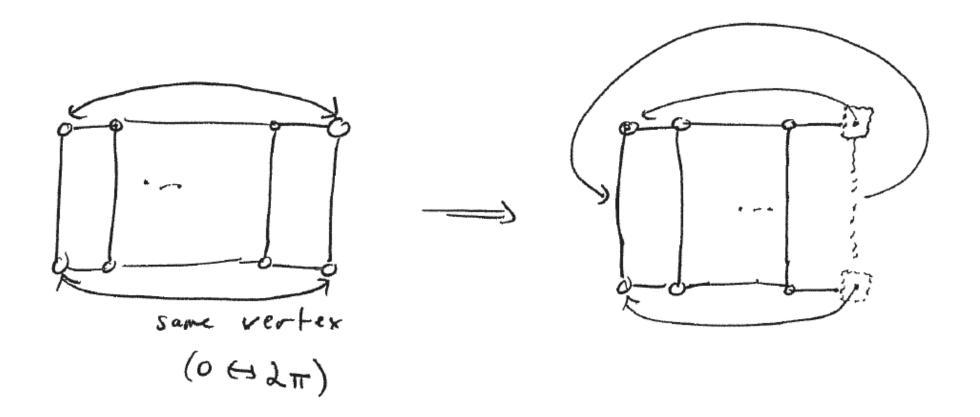


Tessellation



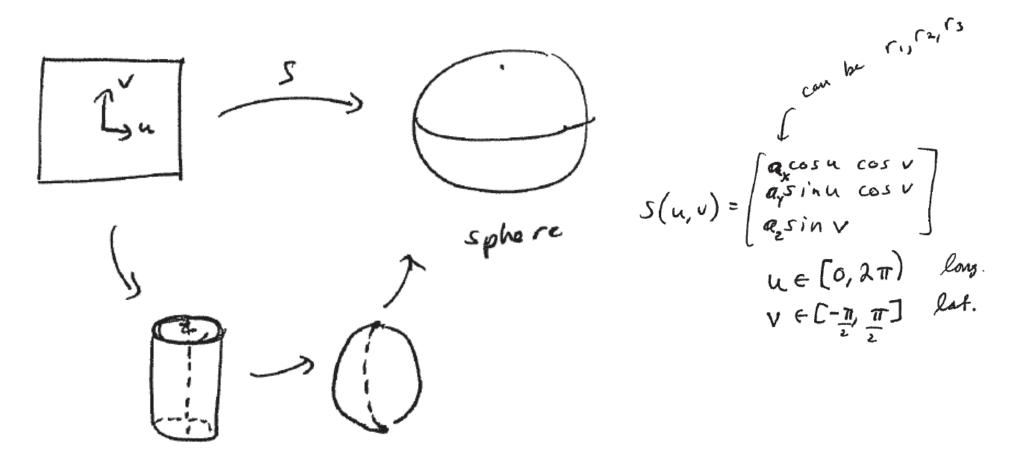
Tessellation

What about the seam?



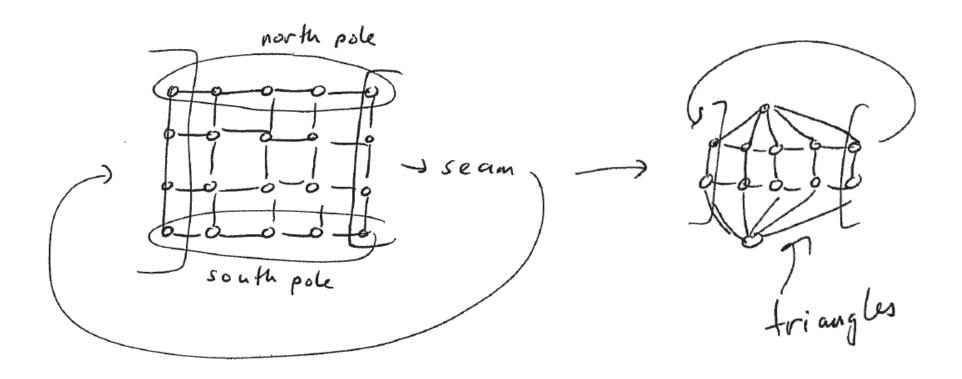
Tessellation

This can get much more complicated



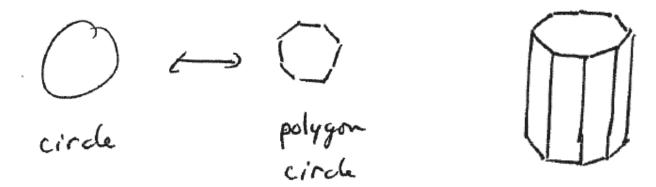
Tessellation

This can get much more complicated

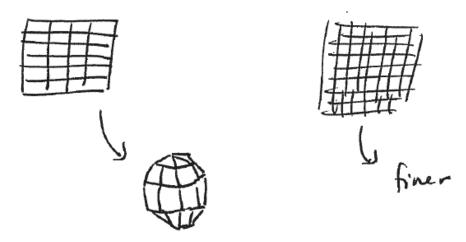


Tessellation resolution

How many points to use?

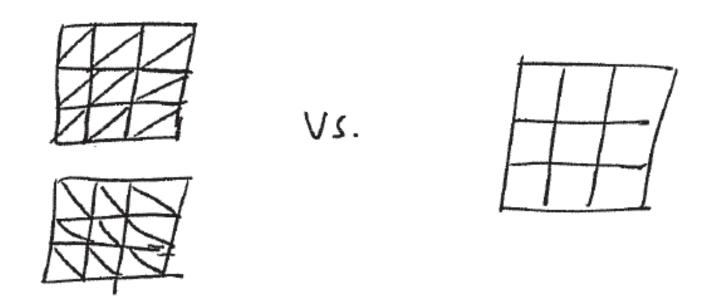


■ How many faces → how fine is the uv grid



Tessellation resolution

Triangles vs. quadrilaterals



- Triangles always planar
- Some triangles collapse in sphere
- Not always planar
- Sometimes better for surface modeling